62. Optical Rotatory Dispersion in the Carbohydrate Group. Part V. Tetramethyl $\gamma$-Gluconolactone.
By R. W. Herbert, E. L. Hirst, H. Samuels, and C. E. Wood.
In marked contrast with tetramethyl $\gamma$-mannonolactone (I), the epimeric $\gamma$-gluconolactone (II) exhibits only small variation in specific rotation when measurements in different solvents are compared (Haworth, Hirst, and Smith, J., 1930, 2659). These two substances differ structurally only in the configurations of the second carbon atoms, and since (I) has been found to display anomalous rotatory dispersion in organic solvents (Part IV, J., 1934, 1825), it was of particular interest to investigate for comparison the optical rotatory dispersion of (II).

The rotation of (I) in organic solvents can be represented by a Drude equation with two terms of opposite sign (see Table I), the frequency constants of which are identifiable with absorbing centres due (a) to the carbonyl group (induced dissymmetry) and (b) to the $\mathrm{C}-\mathrm{C}, \mathrm{C}-\mathrm{O}-$, and $\mathrm{C}-\mathrm{H}$ valencies present in the molecule (bands in the Schumann region). The term ( $\lambda_{2}{ }^{2}=0.06$ ) representing the induced dissymmetry was in this case positive,

Table I.

|  | Tetramethyl $\gamma$-mannonolactone. |  |  |  |  | Tetramethyl $\gamma$-gluconolactone. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{H}_{2} \mathrm{O}$. | EtOH. | $\mathrm{CHCl}_{3}$ | Diox | $\mathrm{C}_{6} \mathrm{H}$ | $\mathrm{H}_{2} \mathrm{O}$. | EtO | CHC | Diox |  |
| $[a]_{\mathrm{D}}$ | $+59 .{ }^{\circ}$ | $-0.78{ }^{\circ}$ | $-3.48^{\circ}$ | $-14.7^{\circ}$ | $-31.7^{\circ}$ | $+59.38^{\circ}$ | $+58.91^{\circ}$ | $+46.60^{\circ}$ | $+65.87^{\circ}$ | $+72.83{ }^{\circ}$ |
| $\lambda_{1}{ }^{2}$ |  | 0.027 | 0.020 | $0 \cdot 022$ | 0.026 | 0.0267 | $7 \quad 0.029$ | 0.035 | 0.034 | 0.035 |
| $\lambda_{2}$ | $0 \cdot 049$ | 0.058 | 0.064 | $0 \cdot 063$ | $0 \cdot 061$ | 0.075 | 0.075 | 0.075 | 0.075 | $0 \cdot 08$ |
| $k_{1}$ |  | $-12.25$ | $-9.84$ | $-13 \cdot 15$ | $-19.04$ | +22.09 | $+19.47$ | +16.53 | $+22.345$ | +23.78 |
| $k_{2}$ | $17 \cdot 8$ | $+10.89$ | $+6.52$ | $+7 \cdot 26$ | $+7.85$ | $-2.56$ | $-0.59$ | $-1.66$ | $-1.35$ | -0.82 |

(The values of $k_{1}$ and $k_{2}$ refer to specific rotations. Full details of the observations summarised above will be found in Part IV and in the experimental section below.)
and the possibility arose that in the methylated $\boldsymbol{\gamma}$-lactones a correlation (comparable with Hudson's rule for the unmethylated $\gamma$-lactones) might exist between the configuration of
(I.)


the carbon atom involved in lactone formation and the sign of the induced dissymmetry. It is clear, however, that the second as well as the fourth carbon atom influences the induced effect, and it appeared probable that by comparing the rotatory dispersion constants of (I) and (II) information would be gained concerning the relative effects of these carbon atoms on the " induced " rotation term.

The experimental results now recorded reveal an unexpected contrast between the dispersions of the two epimerides. In all the solvents investigated (Table I) the rotatory dispersion of tetramethyl $\gamma$-gluconolactone departs comparatively slightly from simplicity and the rotation values are all strongly positive. The deviations from simplicity are sufficiently great to permit of the computation of two-term Drude equations which give satisfactory agreement between the observed and calculated values. Reference to the collected results (Table I) shows that the terms of the Drude equation are opposite in sign and that the positive term is much the greater numerically. This term in all cases has a value for $\lambda_{1}{ }^{2}$ not far removed from 0.035 , corresponding to an absorption band situated approximately at $\lambda 1900$. This wave-length is considerably higher than that of the Schumann band normally associated with $\mathrm{C}-\mathrm{C}, \mathrm{C}-\mathrm{H}$, and $-\mathrm{C}-\mathrm{O}-\mathrm{R}$ linkages which are the origin of the highfrequency term appearing in the rotatory dispersion of tetramethyl $\gamma$-mannonolactone. On the other hand, the wave-length is lower than that of the low-frequency term of the latter lactone ( $\lambda_{2} c a .2500$ ). It is well known, however, that one of the absorption bands of the carboxyl group is situated in this neighbourhood ( $\lambda$ 1900), and it seems probable that the term having $\lambda_{1}{ }^{2}$ ca. 0.035 in the equations for tetramethyl $\gamma$-gluconolactone is to be correlated with the induced dissymmetry of the lactonic carboxyl group. Should this be the case, it follows that in tetramethyl $\gamma$-gluconolactone the induced dissymmetry originating mainly from the fourth carbon atom controls the direction of rotation in all the solvents investigated. In this case, no term with $\lambda^{2} c a .0 .02$ is evident, and it may be concluded that the high-frequency terms contributed by the centres of dissymmetry other than the induced centre almost or entirely cancel out. In contrast with this condition, the ordinary (non-induced) term is important in tetramethyl $\gamma$-mannonolactone, with the result that in the visual region the rotation is positive in some solvents and negative in others. For the latter substance, the value of the induced frequency constant calculated from the rotational data was $\lambda^{2} 0.065$, corresponding with absorption at $\lambda 2500-2600$. It would appear, therefore, that the effect of the cis-methoxy-groups in the methylated mannonolactone is seen in the displacement, relative to its position in the case of the trans-modification, of the absorption wave-length by approximately $600 \AA$. The movement brings the absorption band of tetramethyl $\gamma$-mannonolactone into a position much nearer the characteristic band of the carboxyl group ( $\lambda 2900$ approx.). This difference in the position of the
absorption band may be correlated with another important difference manifested by substances having methoxy-groups respectively cis and trans to one another on carbon atoms 2 and 3. In comparison with their epimerides, all lactones which possess cis-2:3-methoxy- (or hydroxy-) groups are extraordinarily resistant to hydrolysis.

Two points in connexion with the present observations require further discussion. The calculations lead inevitably to the conclusion that a small negative term is present in which $\lambda_{2}{ }^{2}$ has approximately the value $0 \cdot 075$. The origin of this term is obscure, and within the spectral region examined its influence on the total rotation is slight. We have considered its possible association with the carbonyl group of the lactone, but the evidence at present warrants no definite assignment to any particular group, more especially as an exactly similar term has been discovered in the rotatory dispersion of tetramethyl $\alpha$ methylglucoside, a substance having no carboxyl group.

The interpretation suggested above implies that the value of $\lambda$ given by $\lambda_{1}{ }^{2}=0.035$ has a definite physical meaning. This would not be the case if the term were fictitiously simple and in reality represented the sum of two or more terms having different values of $\lambda$. In view of the considerable spectral range covered by several of the sets of observations and the large numerical values of the observed rotations, it seems unlikely that any equation of three or more terms could be found in which $\lambda^{2}$ in the principal term differed appreciably from the value 0.035 . It will be seen from the experimental results that in certain solvents the differences between the observed and calculated values are, although small, greater than the experimental error. It is probable, therefore, that this lactone requires at least a three-term equation to express fully its rotation, but we have been unable to devise any equation in which $\lambda_{1}{ }^{2}$ differs seriously from the value 0.035 .
$2: 3: 5: 6$-Tetramethyl gluconic acid in water, like the corresponding mannonic acid, shows marked general absorption in the near ultra-violet. Within the spectral range available, its rotatory power can be represented by a one-term equation ( $\lambda_{0}{ }^{2}=0.027$ ). The results are recorded in the experimental section, but in view of the small numerical values of $\alpha_{\lambda}$ and the limited spectral range, we reserve for future discussion the interpretation of the values of $\lambda_{0}{ }^{2}$.

## Experimental.

Calculation of the Constants of the Drude Equation.-The following tables show that the deviation from simplicity of the rotatory dispersion of this lactone is slight, amounting to some $12 \%$ of the value of $\alpha_{\lambda}$ at approximately $\lambda 3100$ (see, e.g., data for solutions in dioxan and chloroform). The possible experimental error, although small, is nevertheless an appreciable proportion of this divergence and renders almost impossible the direct calculation of the constants of a two-term Drude equation. Direct calculations (Lowry and Glyn Owen, Trans. Faraday Soc., 1930, 26, 371) made with 4 points, distributed throughout the spectral range investigated, resulted generally in equations the solutions of which involved imaginary quantities.

The method of calculation adopted was to obtain the constant, $\lambda_{1}$, of an approximate oneterm equation by careful extrapolation of the graph of $1 / \alpha$ against $\lambda^{2}$. A value for $\lambda_{2}$ was then assumed, and four experimental points, A, B, C and D, were chosen, distributed as evenly as possible throughout the spectral range examined, measurements having been taken to the limits of transparency in a $2-\mathrm{dm}$. tube. By using these values of $\lambda_{1}$ and $\lambda_{2}$, values of $k_{1}$ and $k_{2}$ were computed from the experimental points A and C, and a second pair, $k_{1}{ }^{\prime}$ and $k_{2}{ }^{\prime}$, from the points B and D . If $\lambda_{1}$ and $\lambda_{2}$ had been correctly chosen, it would be found that $k_{1}=k_{1}{ }^{\prime}$ and $k_{2}=k_{2}{ }^{\prime}$ within the experimental error, but in general this would not be the case, so $\lambda_{1}$ was then varied by trial and error until the differences $k_{1}-k_{1}^{\prime}$ and $k_{2}-k_{2}^{\prime}$ were as small as possible; then $\lambda_{2}$ was varied with the same object, and finally, by repeating the whole process of successive approximation as often as necessary, the variation of $k_{1}$ and $k_{2}$ over the whole dispersion curve was reduced to less than the experimental error or to a minimum.

This method of obtaining a two-term ( 4 constant) Drude equation seems to be the only one available where variations from simplicity are small. The signs of $k_{1}$ and $k_{2}$ are readily ascertainable in the preliminary stage of the calculation, but the ultimate exact evaluation of $\lambda_{1}$ and $\lambda_{2}$ and consequent values of $k_{1}$ and $k_{2}$ is a very long process.

It will be noted that the frequency constants $\left(\lambda_{1}\right)$ of the most satisfactory simple equations which are given for comparison) are less than the corresponding constants ( $\lambda_{1}$ ) of the highfrequency term in the complex equations, and that the deviation from simplicity ( $\alpha$, obs. $-\alpha$,
calc.) is negative. It was found possible to derive more than one equation which gave reasonably close agreement between observed and calculated values. The possible variations in $\lambda_{1}{ }^{2}$
 and $\lambda_{2}{ }^{2}$ are, however, inconsiderable, and there is no escape from the introduction of terms containing respectively a value of $\lambda_{2}{ }^{2}$ not far removed from 0.07 and of $\lambda_{1}{ }^{2}$ close to $0 \cdot 035$. This applies even for those alternative equations (the best of several calculated) given for the dioxan and benzene solutions of the lactone, none of which is within our recognised limits of experimental error. It is highly probable, however, that the rotation of this lactone requires a more complicated function for its exact representation. Attempts were made to follow the dispersion curves into the region of absorption, but even with $2-\mathrm{cm}$. columns of solution the absorption was too great to permit accurate observations. Photometric measurements on solutions of the lactone in water, alcohol, and dioxan showed slight absorption between $\lambda 7000$ and $\lambda 3000$. Beyond $\lambda 3000$, general absorption set in, rising steeply at about $\lambda 2700$. There was no indication of selective absorption (see fig.).

Rotatory Dispersion.-Tetramethyl $\gamma$-gluconolactone was prepared by the oxidation of tetramethyl glucofuranose (see Drew, Goodyear, and Haworth, J., 1927, 1237). It was purified for the present work by several successive distillations in a vacuum; b. p. $97^{\circ} / 0.05 \mathrm{~mm} ., \mathrm{m}$. p. $27^{\circ}$. The rotational measurements were made by the methods given in Part I (J., 1930, 2108).
$D=$ Algebraical difference between observed and calculated values.
2:3:5:6-Tetramethyl gluconic acid in water: $c=7.228 ; t=20^{\circ} ; l=2 \mathrm{dm} . ; \quad[\alpha]_{\lambda}^{20}=$ $6.917 \alpha_{\lambda} ; \quad[\alpha]_{\mathrm{D}}^{20^{\circ}}=22.90^{\circ} ; \quad \alpha_{\lambda}=1.06 /\left(\lambda^{2}-0.027\right)$.

| $\lambda$. | $a$, obs. | $D$. | $\lambda$. | $a$, obs. | $D$. | $\lambda$. | $a$, obs. | $D$. | $\lambda$. | $a$, obs. | $D$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6708 | $+2.57^{\circ}$ | +0.06 | 5515 | $+3.82^{\circ}$ | $\pm 0$ | 4538 | $+5.91^{\circ}$ | -0.01 | 4010 | $+7.91^{\circ}$ | -0.01 |
| 6292 | 2.87 | $\pm 0$ | 5225 | $4 \cdot 31$ | $\pm 0$ | 4376 | 6.41 | -0.03 | 3920 | 8.41 | +0.04 |
| 5893 | 3.31 | $\pm 0$ | 4887 | 4.98 | -0.02 | 4258 | 6.91 | +0.04 | 3749 | 9.41 | +0.05 |
| 5805 | 3.39 | -0.03 | 4736 | 5.41 | +0.04 | 4130 | 7.41 | +0.03 | 3582 | 10.41 | -0.05 |

2:3:5:6-Tetramethylgluconolactone.-In water: $c=8.016 ; t=20^{\circ} ; l=2 \mathrm{dm} . ;[\alpha]_{\lambda}^{20^{\circ}}=$ $6.238 \alpha_{\lambda} ; \quad[\alpha]_{\mathrm{D}}^{20^{\circ}}=59.38^{\circ} ; \quad \alpha_{\lambda}=3.54097 /\left(\lambda^{2}-0.0267\right)-0.410224 /\left(\lambda^{2}-0.075\right)$.

| 6708 | $+7.24^{\circ}$ | -0.03 | 5225 | $+12.24^{\circ}-0.07$ | 4376 | $+17.91^{\circ}-0.06$ | 3720 | $+25.41^{\circ}$ | +0.17 |  |  |
| :--- | ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6292 | 8.30 | -0.01 | 4887 | 14.10 | -0.09 | 4216 | 19.41 | -0.04 | 3601 | 26.91 | +0.02 |
| 6104 | 8.86 | $\pm 0$ | 4844 | 14.41 | -0.05 | 4072 | 20.91 | -0.03 | 3498 | 28.41 | +0.05 |
| 5893 | 9.52 | -0.02 | 4694 | 15.41 | -0.06 | 3952 | 22.41 | +0.11 | 3352 | 30.41 | +0.05 |
| 5805 | 9.81 | -0.03 | 4568 | 16.41 | +0.02 | $\mathbf{3 8 2 2}$ | 23.91 | +0.02 | 3200 | 32.41 | +0.60 |

In alcohol : $c=11.2112 ; \quad t=25^{\circ} ; \quad l=2 \mathrm{dm} . ; \quad[\alpha]_{\lambda}^{25^{\circ}}=4.46 \alpha_{\lambda} ; \quad[\alpha]_{\mathrm{D}}^{25^{\circ}}=58.91^{\circ} ; \quad \alpha_{\lambda}=$ $4.365853 /\left(\lambda^{2}-0.02895\right)-0 \cdot 131958 /\left(\lambda^{2}-0.075\right)$.

| 6708 | $+10.01^{\circ}$ | -0.01 | 5515 | $+15 \cdot 29^{\circ}$ | +0.01 | 4354 | $+26.04^{\circ}$ | $\pm 0$ | 3581 | $+41.644^{\circ}$ | +0.15 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6292 | 11.45 | -0.04 | 5225 | 17.22 | $\pm 0$ | 4099 | 30.04 | $\pm 0.07$ | 3453 | 45.44 | +0.06 |
| 6104 | 12.23 | -0.03 | 4886 | 20.04 | +0.04 | 3898 | 33.84 | +0.05 | 3318 | 50.04 | -0.01 |
| 5805 | 13.62 | -0.05 | 4682 | 22.04 | +0.01 | 3786 | 36.24 | $\pm 0$ | 3235 | 52.44 | -0.22 |

In chloroform: $\quad c=7.586 ; \quad t=25^{\circ} ; \quad l=2 \mathrm{dm} . ; \quad[\alpha]_{\lambda}^{20^{\circ}}=6.591 \alpha_{\lambda} ; \quad[\alpha]_{5^{20}}=46.60$; $\alpha_{\lambda}=2.5082 /\left(\lambda^{2}-0.0346\right)-0.251375 /\left(\lambda^{2}-0.075\right) \quad$ (Equation A); $\quad \alpha_{\lambda}=2.262 /\left(\lambda^{2}-0.028\right)$ Equation B).
$\begin{array}{ll}\text { Diff. } & \text { Diff. } \\ \text { (A). } & \text { (B). }\end{array}$

| $\lambda$. | $a$, obs. | (A). | (B). |
| :---: | :---: | :---: | :---: |
| 6708 | $+5 \cdot 40^{\circ}$ | $+0.03^{\circ}$ | $+0.04^{\circ}$ |
| 6292 | 6.15 | -0.01 | $\pm 0$ |
| 6104 | 6.54 | -0.04 | $\pm 0.03$ |
| 5893 | 7.07 | +0.03 | -0.01 |
| 5805 | 7.32 |  | -0.01 |
| 5515 | 8.20 |  | -0.01 |
|  | +0.01 |  |  |

$\lambda . \quad a$, obs. (A). $\quad \begin{array}{ll}\text { (B). }\end{array}$ $\begin{array}{lccl}5225 & +9.23^{\circ} & -0.02^{\circ} \pm 0^{\circ} \\ 4887 & 10.73 & -0.02 & \pm 0 \\ 4589 & 12.41 & +0.01 & \pm 0.01 \\ 4360 & 13.91 & -0.04 & -0.04 \\ 4179 & 15.41 & +0.02 & -0.02 \\ 4000 & 17.01 & -0.03 & -0.13\end{array}$

| $\lambda$. | $a$, obs. | Diff. <br> (A). | Diff. <br> (B). |
| :---: | :---: | :---: | :---: |
| 3821 | $+19.01^{\circ}$ | $+0.03^{\circ}-0.16$ |  |
| 3660 | 21.01 | +0.03 | -0.34 |
| 3514 | 23.01 | -0.03 | -0.68 |
| 3322 | 26.01 | +0.01 | -1.46 |
| 3188 | 28.01 | +0.03 | -2.71 |
| 3107 | 29.21 | +0.38 | -3.80 |

In dioxan: $\quad c=11.416 ; \quad t=25^{\circ} ; \quad l=2 \mathrm{dm} . ; \quad[\alpha]_{\lambda}^{25^{\circ}}=4 \cdot 38 \alpha_{\lambda} ; \quad[\alpha]_{\mathrm{D}}^{25^{\circ}}=65 \cdot 87^{\circ} ; \alpha_{\lambda}=$ $5 \cdot 10172 /\left(\lambda^{2}-0.03415\right)-0.337626 /\left(\lambda^{2}-0.075\right)$ (Equation $\left.A\right) ; \alpha_{\lambda}=5.04994 /\left(\lambda^{2}-0.0333\right)-$ $0.282324 /\left(\lambda^{2}-0.075\right)$ (Equation B) ; $\alpha_{\lambda}=4.73 /\left(\lambda^{2}-0.032\right)$ (Equation C).

| $\lambda$. | $a$, obs. | Diff. (A). | Diff. (B). | Diff. (C.) | $\lambda$. | $a$, obs. | Diff. (A). | Diff. (B). | Diff. (C). |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6708 | $+11.35^{\circ}$ | $-0.02^{\circ}$ | $-0.02^{\circ}$ | $+0.03^{\circ}$ | 4101 | $+34.43{ }^{\circ}$ | $-0.01^{\circ}$ | $+0.02^{\circ}$ | $-0.30^{\circ}$ |
| 6292 | 13.03 | $-0.02$ | -0.02 | $+0.03$ | 3983 | 37.08 | $+0 \cdot 11$ | +0.17 | -0.27 |
| 6104 | 13.91 | $-0.02$ | -0.02 | $+0.02$ | 3850 | $40 \cdot 06$ | $\pm 0$ | -0.02 | -0.64 |
| 5893 | 15.04 | -0.01 | $\pm 0$ | $+0.04$ | 3720 | $43 \cdot 46$ | -0.15 | -0.14 | $-1 \cdot 00$ |
| 5805 | 15.52 | -0.04 | -0.03 | $+0.01$ | 3588 | $47 \cdot 64$ | -0.02 | -0.02 | -1.26 |
| 5515 | $17 \cdot 42$ | -0.01 | $+0.01$ | $+0.04$ | 3520 | 50.04 | +0.10 | $+0.07$ | -1.43 |
| 5225 | $19 \cdot 60$ | -0.05 | -0.04 | $-0.03$ | 3444 | $52 \cdot 64$ | $+0.02$ | -0.08 | -1.97 |
| 4887 | $22 \cdot 84$ | $-0.03$ | -0.01 | $-0.03$ | 3364 | $55 \cdot 64$ | -0.08 | $-0.19$ | -2.64 |
| 4681 | $25 \cdot 27$ | $+0.03$ | $+0.05$ | -0.01 | 3285 | 58.84 | -0.06 | $-0 \cdot 26$ | $-3.47$ |
| 4564 | 26.84 | +0.08 | $+0 \cdot 10$ | $+0.01$ | 3200 | 62.44 | +0.01 | -0.34 | -4.75 |
| 4445 | 28.44 | $-0.03$ | $\pm 0$ | $-0.13$ | 3144 | $64 \cdot 84$ | $+0.15$ | -0.36 | $-5.92$ |
| 4259 | 31.44 | -0.04 | $-0.01$ | -0.22 | 3097 | $67 \cdot 24$ | +0.78 | $+0.09$ | $-6.77$ |
| 4216 | 32.28 | $+0.04$ | $+0.07$ | $-0.17$ | 3020 | $69 \cdot 64$ | +1.05 | -0.15 | -10.25 |

In benzene : $c=10.662 ; t=25^{\circ} ; \quad l=2 \mathrm{dm} . ; \quad[\alpha]_{\lambda}^{25^{\circ}}=4.6896 \alpha_{\lambda} ; \quad[\alpha]_{\mathrm{D}}^{25^{\circ}}=72.83^{\circ} ; \alpha_{\lambda}=$ $5.354337 /\left(\lambda^{2}-0.0398\right)-0.511828 /\left(\lambda^{2}-0.075\right) \quad$ (Equation $\left.\quad A\right) ; \quad \alpha_{\lambda}=5.07 /\left(\lambda^{2}-0.035\right)-$ $0 \cdot 175 /\left(\lambda^{2}-0.08\right)$ (Equation B).

| $\lambda$. | $a$, obs. | Diff. <br> (A). | Diff. (B). | $\lambda$. | $a$, obs. | Diff. (A). | Diff. (B). | $\lambda$. | a, obs. | Diff. (A). | Diff. (B). |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6708 | $+11.76^{\circ}$ | $+0.07^{\circ}$ | $+0.01^{\circ}$ | 4755 | $+25.41^{\circ}$ | $+0.06^{\circ}$ | $+0.08^{\circ}$ | 3694 | $+46.91^{\circ}$ | -0.15 ${ }^{\circ}$ | $+0.04^{\circ}$ |
| 6270 | 13.52 | $-0.02$ | $-0.08$ | 4603 | $27 \cdot 41$ | +0.03 | $+0.08$ | 3622 | $49 \cdot 41$ | -0.07 | +0.13 |
| 6104 | 14.35 | -0.02 | $-0.07$ | 4472 | $29 \cdot 41$ | $+0.07$ | $+0 \cdot 14$ | 3551 | 51.91 | -0.12 | $+0.05$ |
| 5880 | $15 \cdot 63$ | $+0.02$ | $-0.03$ | 4293 | $32 \cdot 41$ | $+0.04$ | $+0 \cdot 13$ | 3488 | 54.41 | -0.03 | +0.11 |
| 5805 | 16.08 | $-0.01$ | $-0.03$ | 4090 | $36 \cdot 41$ | -0.04 | $+0.09$ | 3415 | 57.41 | $+0.01$ | $+0.07$ |
| 5515 | $18 \cdot 00$ | -0.02 | $-0.05$ | 3957 | $39 \cdot 41$ | $-0 \cdot 17$ | $\pm 0 \cdot 00$ | 3345 | $60 \cdot 41$ | +0.01 | -0.04 |
| 5225 | $20 \cdot 35$ | $-0.03$ | -0.04 | 3774 | $44 \cdot 41$ | -0.17 | $\mp 0 \cdot 12$ | 3259 | $64 \cdot 41$ | +0.19 | $-0.11$ |
| 4887 | 23.75 | $-0.03$ | -0.02 | 3709 | $46 \cdot 41$ | -0.18 | $+0.03$ | 3190 | $67 \cdot 41$ | $+0 \cdot 13$ | -0.49 |

The authors thank Imperial Chemical Industries Limited for financial assistance.
University of Birmingham, Edgbaston.
[Received, December 21st, 1934.]

